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## DEFAULT PROPENSITY IMPLICIT IN PULLED TO PAR V@R FOR BONDS

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This work is dedicated to Roman Zmyslony as a token of gratitude for his joy and enthusiasm in the productive research collaborations he actively promoted between Poland and Portugal.

> Whatever way we keep looking at bond prices there is no diffusion model that works. – Pedro Corte Real, Cofounder at MAGENTAKONCEPT, Lda, Portugal.

## Abstract

Using the *pulled to par* returns, proposed by [27] for computing historical V@R of bonds, we develop a way of extracting – at any reference date before maturity – *implicit default propensities* from observed bond quotes. This method is new to the literature and it has the advantage on focusing directly on loss given default.

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To illustrate the method we present two examples of actual computation with real data – on German and Portuguese bonds. The market data seems to support the proposed method.

In the case of a very concrete simple Gaussian model, we establish the connection between our *implicit default propensity* and the more traditional notions of *default probability* and *recovery given default* of a bond.

**Keywords:** value-at-risk, bonds, default probability, recovery given default.

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