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DISCRETE APPROXIMATIONS OF GENERALIZED RBSDE WITH RANDOM TERMINAL TIME

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Abstract

The convergence of discrete approximations of generalized reflected backward stochastic differential equations with random terminal time in a general convex domain is studied. Applications to investigation obstacle elliptic problem with Neumann boundary condition for partial differential equations are given.

Keywords: generalized reflected BSDE, discrete approximation methods, viscosity solution.

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