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ON THE UNIVERSAL CONSTANT IN THE KATZ-PETROV AND OSIPOV INEQUALITIES *

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Abstract

Upper estimates are presented for the universal constant in the Katz-Petrov and Osipov inequalities which do not exceed 3.1905.

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