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ON THE OPTIMAL CONTINUOUS EXPERIMENTAL DESIGN PROBLEM

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Abstract

The target of this paper is to provide a compact review of the Optimal Experimental Design, the continuous case. Therefore we are referring to the general nonlinear problem in comparison to the linear one.

Keywords: nonlinear experimental design, static, sequential design.

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