

[Full PDF](#)

[DMPS Page](#)

*Discussiones Mathematicae
Probability and Statistics 30 (2010) 5–19
doi:10.7151/dmps.1118*

AN ASYMPTOTICALLY UNBIASED MOMENT ESTIMATOR OF A NEGATIVE EXTREME VALUE INDEX*

FREDERICO CAEIRO

DM and CMA

*Faculdade de Ciências e Tecnologia
Universidade Nova de Lisboa
2829–516 Caparica, Portugal*

e-mail: fac@fct.unl.pt

AND

M. IVETTE GOMES

*DEIO and CEAUL
Faculdade de Ciências
Universidade de Lisboa
1749–016 Lisboa, Portugal*

e-mail: ivette.gomes@fc.ul.pt

*In honour of Professor João Tiago Mexia on the occasion of his seventieth
birthday*

Abstract

In this paper we consider a new class of consistent semi-parametric estimators of a negative extreme value index, based on the set of the k largest observations. This class of estimators depends on a control or tuning parameter, which enables us to have access to an estimator with a null second-order component of asymptotic bias, and with a rather interesting mean squared error, as a function of k .

*This work was partially supported by FCT/MCTES/PT,FCT/POCTI,POCI 2010 and PPDCT/FEDER.

We study the consistency and asymptotic normality of the proposed estimators. Their finite sample behaviour is obtained through Monte Carlo simulation.

Keywords: extreme value index, semi-parametric estimation; moment estimator.

2010 Mathematics Subject Classification: Primary 62G32, 62E20; Secondary 65C05.

REFERENCES

- [1] F. Caeiro, M.I. Gomes and D.D. Pestana, *Direct reduction of bias of the classical Hill estimator*, Revstat **3** (2) (2005), 113–136.
- [2] A.L.M. Dekkers, J.H.J. Einmahl and L. de Haan, *A moment estimator for the index of an extreme-value distribution*, The Annals of Statistics **17** (4) (1989), 1833–1855. doi:10.1214/aos/1176347397
- [3] G. Draisma, L. de Haan, L. Peng and T. Themido Pereira, *A bootstrap-based method to achieve optimality in estimating the extreme value index*, Extremes **2** (4) (1999), 367–404. doi:10.1023/A:1009900215680
- [4] M.I. Fraga Alves, *Weiss-Hill estimator*, Test **10** (2001), 203–224. doi:10.1007/BF02595832
- [5] B.V. Gnedenko, *Sur la distribution limite du terme maximum d'une série aléatoire*, Ann. Math. **44** (1943), 423–453. doi:10.2307/1968974
- [6] M.I. Gomes, L. de Haan and L. Henriques Rodrigues, *Tail Index estimation for heavy-tailed models: accommodation of bias in weighted log-excesses*, J. R. Stat. Soc. Ser. B **70** (1) (2008), 31–52.
- [7] M.I. Gomes, M.J. Martins and M.M. Neves, *Improving second order reduced-bias tail index estimation*, Revstat **5** (2) (2007), 177–207.
- [8] M.I. Gomes and C. Neves, *Asymptotic comparison of the mixed moment and classical extreme value index estimators*, Statistics & Probability Letters **78** (2008), 643–653. doi:10.1016/j.spl.2007.07.026
- [9] M.I. Gomes and O. Oliveira, *The bootstrap methodology in Statistics of Extremes - choice of the optimal sample fraction*, Extremes **4** (4) (2001), 331–358. doi:10.1023/A:1016592028871
- [10] L. de Haan, *On Regular Variation and its Application to the Weak Convergence of Sample Extremes*, Mathematical Centre Tract 32, Amsterdam 1970.
- [11] L. de Haan and A. Ferreira, *Extreme Value Theory: an Introduction*, Springer New York 2006.

- [12] B.M. Hill, *A Simple General Approach to Inference About the Tail of a Distribution*, The Annals of Statistics **3** (5) (1975), 1163–1174.
doi:10.1214/aos/1176343247

Received 12 February 2010