

**EXISTENCE AND UNIQUENESS OF SOLUTIONS FOR A
FRACTIONAL p -LAPLACIAN PROBLEM IN \mathbb{R}^N**

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Abstract

In this article, we use the Browder-Minty theorem to establish the existence and uniqueness of a weak solution for a fractional p -Laplace equation in \mathbb{R}^N .

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