

POINTWISE STRONG APPROXIMATION OF ALMOST PERIODIC FUNCTIONS

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Abstract

We consider the class $GM(2\beta)$ in pointwise estimate of the deviations in strong mean of almost periodic functions from matrix means of partial sums of their Fourier series.

Keywords: almost periodic functions, rate of strong approximation, summability of Fourier series.

2010 Mathematics Subject Classification: 42A24.

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Received 26 January 2016

Revised 1 March 2016