

## SPACES OF LIPSCHITZ FUNCTIONS ON METRIC SPACES

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*Dedicated to Zbigniew Semadeni, the founder of Categorical Functional Analysis*

### Abstract

In this paper the universal properties of spaces of Lipschitz functions, defined over metric spaces, are investigated.

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