

## SOME AVERAGING RESULTS FOR ORDINARY DIFFERENTIAL INCLUSIONS

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### Abstract

We consider ordinary differential inclusions and we state and discuss some averaging results for these inclusions. Our results are proved under weaker conditions than the results in the literature.

**Keywords:** ordinary differential inclusions, averaging method.

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