

EXISTENCE RESULTS FOR DELAY SECOND ORDER DIFFERENTIAL INCLUSIONS

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Abstract

In this paper, some fixed point principle is applied to prove the existence of solutions for delay second order differential inclusions with three-point boundary conditions in the context of a separable Banach space. A topological property of the solutions set is also established.

Keywords: boundary-value problems, delay differential inclusions, fixed point, retract.

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