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ON COMMUTATIVITY OF PROJECTORS

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Dedicated to the memory of Jerzy K. Baksalary

Abstract

It is shown that commutativity of two oblique projectors is equivalent with their product idempotency if both projectors are not necessarily Hermitian but orthogonal with respect to the same inner product.

Keywords: oblique projector, orthogonal projector, commutativity.

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