

IMPLICATION ALGEBRAS

IVAN CHAJDA

Department of Algebra and Geometry
Palacký University of Olomouc
Tomkova 40, 779 00 Olomouc, Czech Republic

e-mail: chajda@risc.upol.cz

Abstract

We introduce the concepts of pre-implication algebra and implication algebra based on orthosemilattices which generalize the concepts of implication algebra, orthoimplication algebra defined by J.C. Abbott [2] and orthomodular implication algebra introduced by the author with his collaborators. For our algebras we get new axiom systems compatible with that of an implication algebra. This unified approach enables us to compare the mentioned algebras and apply a unified treatment of congruence properties.

Keywords: implication algebra, pre-implication algebra, orthoimplication algebra, orthosemilattice, congruence kernel.

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