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PROPERTIES OF SET-VALUED STOCHASTIC INTEGRALS

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Abstract

We introduce set-valued stochastic integrals driven by a square-integrable martingale and by a semimartingale. We investigate properties of both integrals.

Keywords: decomposable set, Hausdorff metric, predictable set-valued process, square-integrable martingale, semimartingale.

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