

## SET-VALUED STRATONOVICH INTEGRAL

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### Abstract

The purpose of the paper is to introduce a *set-valued Stratonovich integral* driven by a one-dimensional Brownian motion. We discuss the existence of this integral and investigate its properties.

**Keywords:** set-valued function, Hukuhara differential, selection of a set-valued map, semimartingale, Stratonovich integral.

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