

IMPROVED SUFFICIENT CONDITIONS FOR HAMILTONIAN PROPERTIES

JENS-P. BODE¹, ANIKA FRICKE²

AND

ARNFRIED KEMNITZ¹

¹*Computational Mathematics*
Technische Universität Braunschweig
38092 Braunschweig, Germany

²*Zentrum für erfolgreiches Lehren und Lernen*
Ostfalia Hochschule für angewandte Wissenschaften
38302 Wolfenbüttel, Germany

e-mail: jp.bode@tu-bs.de
Anika.Fricke@ostfalia.de
a.kemnitz@tu-bs.de

Abstract

In 1980 Bondy [2] proved that a $(k+s)$ -connected graph of order $n \geq 3$ is traceable ($s = -1$) or Hamiltonian ($s = 0$) or Hamiltonian-connected ($s = 1$) if the degree sum of every set of $k+1$ pairwise nonadjacent vertices is at least $((k+1)(n+s-1)+1)/2$. It is shown in [1] that one can allow exceptional $(k+1)$ -sets violating this condition and still implying the considered Hamiltonian property. In this note we generalize this result for $s = -1$ and $s = 0$ and graphs that fulfill a certain connectivity condition.

Keywords: Hamiltonian, traceable, Hamiltonian-connected.

2010 Mathematics Subject Classification: 05C45.

REFERENCES

- [1] J.-P. Bode, A. Kemnitz, I. Schiermeyer and A. Schwarz, *Generalizing Bondy's theorems on sufficient conditions for Hamiltonian properties*, Congr. Numer. **203** (2010) 5–13.
- [2] J.A. Bondy, Longest paths and cycles in graphs of high degree, Research Report CORR 80-16 (Department of Combinatorics and Optimization, Faculty of Mathematics, University of Waterloo, Waterloo, Ontario, Canada, 1980).
- [3] J.A. Bondy and V. Chvátal, *A method in graph theory*, Discrete Math. **15** (1976) 111–135.
doi:10.1016/0012-365X(76)90078-9
- [4] V. Chvátal and P. Erdős, *A note on Hamiltonian circuits*, Discrete Math. **2** (1972) 111–113.
doi:10.1016/0012-365X(72)90079-9
- [5] G.A. Dirac, *Some theorems on abstract graphs*, Proc. London Math. Soc. **s3-2** (1952) 69–81.
doi:10.1112/plms/s3-2.1.69
- [6] P. Fraisse, D_λ -cycles and their applications for Hamiltonian graphs (LRI, Rapport de Recherche **276**, Centre d'Orsay, Université de Paris-Sud, 1986).
- [7] O. Ore, *Note on Hamiltonian circuits*, Amer. Math. Monthly **67** (1960) 55.
- [8] O. Ore, *Hamilton connected graphs*, J. Math. Pures Appl. **42** (1963) 21–27.

Received 20 January 2014
Revised 3 September 2014
Accepted 3 September 2014