

## AN IMPLICIT WEIGHTED DEGREE CONDITION FOR HEAVY CYCLES<sup>1</sup>

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### Abstract

For a vertex  $v$  in a weighted graph  $G$ ,  $id^w(v)$  denotes the implicit weighted degree of  $v$ . In this paper, we obtain the following result: Let  $G$  be a 2-connected weighted graph which satisfies the following conditions: (a) The implicit weighted degree sum of any three independent vertices is at least  $t$ ; (b)  $w(xz) = w(yz)$  for every vertex  $z \in N(x) \cap N(y)$  with  $xy \notin E(G)$ ; (c) In every triangle  $T$  of  $G$ , either all edges of  $T$  have different weights or all edges of  $T$  have the same weight. Then  $G$  contains either a hamiltonian cycle or a cycle of weight at least  $2t/3$ . This generalizes the result of Zhang *et al.* [9].

**Keywords:** weighted graph, hamiltonian cycles, heavy cycles, implicit degree, implicit weighted degree.

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